





### **Essential** Question

**HOW does measurement** help you solve problems in everyday life?



### **Common Core** GPS

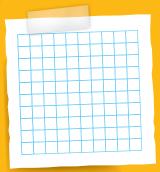
**Content Standards** MCC6.G.1, MCC6.G.3, MCC6.NS.8

**Mathematical Practices** 1, 2, 3, 4, 5, 6, 7, 8



### Math in the **Real World**

**Gardens** A garden designer plants dahlias in a 5 foot by 3 foot plot. What area of the garden do the dahlias cover? In the diagram below, shade the area covered by dahlias.



Area =



Study Organizer

Cut out the correct Foldable from the FL pages in the back of this book.



Place your Foldable on the Key Concept page toward the end of this chapter.



Use the Foldable throughout this chapter to help you learn about area.



## Vocabulary

base height

composite figure parallelogram

congruent polygon rhombus formula

## **Review Vocabulary**

Using a graphic organizer can help you to remember important vocabulary terms. Fill in the graphic organizer below for the word area.

Area

Definition

Units of Measure

Real-World Examples

## When Will You Use This?







Common Core Review MCC4.MD.3, MCC5.NF.4

## Example 1

Find the area of the rectangle.



$$A = \ell w$$
 Area of a rectangle

$$A = 9 \cdot 6$$
 Replace  $\ell$  with 9 and  $w$  with 6.

$$A = 54$$
 Multiply.

The area of the rectangle is 54 square feet.

### Example 2

Find  $\frac{1}{2} \times 16$ .

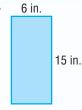
$$\frac{1}{2} \times 16 = \frac{1}{2} \times \frac{16}{1}$$
 Write 16 as  $\frac{16}{1}$ .
$$= \frac{1 \times 16}{2 \times 1}$$
 Divide the numerator and the denominator by 2.
$$= \frac{8}{1} \text{ or } 8$$
 Simplify.

### Quick Check

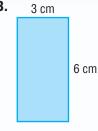
Area Find the area of each rectangle.

1. 8 cm





3.



4. The playing area of a board game is a rectangle with a length of 14 inches and a width of 20 inches. What is the area of the board game?

Fractions Multiply. Write in simplest form.

**5.** 
$$\frac{1}{2} \times 28 =$$

**5.** 
$$\frac{1}{2} \times 28 =$$
 **6.**  $\frac{1}{3} \times 27 =$  **7.**  $\frac{1}{7} \times 84 =$ 

$$\{ 7. \frac{1}{7} \times 84 = \underline{\hspace{1cm}}$$



Which problems did you answer correctly in the Quick Check? Shade those exercise numbers below.

- 1

HOW does finding the area of a parallelogram relate to finding the area of a rectangle?



Mathematical **Practices** 1, 2, 3, 5

**Banners** Elise wants to make a banner in the shape of a parallelogram. Her parallelogram has a base of 3 feet and a height of 2 feet. What is the area of her parallelogram?

## Investigation 1

Another type of quadrilateral is a parallelogram. A parallelogram has opposite sides parallel and congruent.

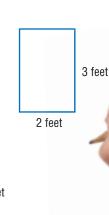
Parallelograms	Not Parallelograms

Make a parallelogram to represent Elise's banner.

Step 1

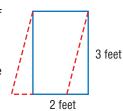
Start with a rectangle.

Trace the rectangle shown at the right.



Step 2

Cut a triangle from one side of the rectangle you traced and move it to the other side to form a parallelogram. Tape the parallelogram to the right.



The rectangle was rearranged to form the parallelogram. Nothing was removed or added, so the parallelogram has area as the rectangle.

Step 3

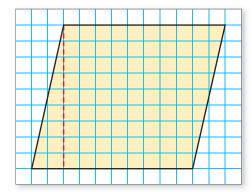
Find the base and height of the parallelogram to find the area. The base of the parallelogram is 2 feet and the height is 3 feet.

feet x feet = square feet

## Investigation 2

Find the area of the parallelogram below.

Step 1 Trace the parallelogram on grid paper and cut it out.



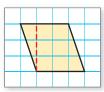
- Step 2 Fold and cut along the dotted line.
- Move the triangle to the right to make a rectangle. Tape the rectangle in the space provided.
- Step 4 Count the number of square units in the rectangle.

The area is square units.

## Investigation 3

Find the area of the parallelogram below.

Step 1 Trace the parallelogram and cut it out.



Step 2 Fold and cut along the dotted line. Then move the triangle to the right to make a rectangle.

Tape it in the space provided.



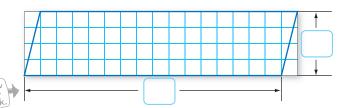
**Step 3** Count the number of square units in the rectangle.

The area is square units.

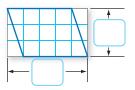


## Use Math Tools Work with a partner. Find the area of each parallelogram.

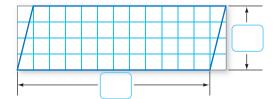
**1.** A =\_\_\_\_\_ square units



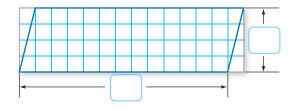
**2.** A = \_\_\_\_\_ square units



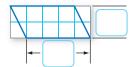
**3.** A = \_\_\_\_\_ square units



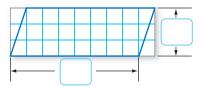
**4.** A = \_\_\_\_\_ square units



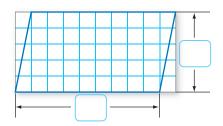
**5.** A = \_\_\_\_\_ square units



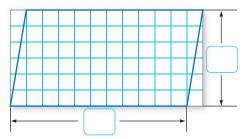
**6.** A = \_\_\_\_\_ square units



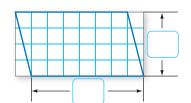
7. A = square units



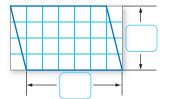
**8.** A = \_\_\_\_\_ square units



**9.** A = \_\_\_\_\_ square units



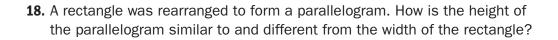
**10.** *A* = \_\_\_\_\_ square units





The table shows the dimensions of several rectangles and the corresponding dimensions of several parallelograms if each rectangle was rearranged to form a parallelogram. Work with a partner to complete the table. The first one is done for you.

	Rectangle	Length (ℓ)	Width (w)	Parallelogram	Base (b)	Height (h)	Area (units <sup>2</sup> )
	Rectangle 1	6	2	Parallelogram 1	6	2	12
11.	Rectangle 2	12	4	Parallelogram 2			
12.	Rectangle 3	7	3	Parallelogram 3			
13.	Rectangle 4	5	4	Parallelogram 4			
14.	Rectangle 5	10	6	Parallelogram 5			
15.	Rectangle 6	6	4	Parallelogram 6			
16.	Rectangle 7	15	9	Parallelogram 7			
17.	Rectangle 8	9	3	Parallelogram 8			



19.	CEPS	Reason Inductively	Write a rule that gives the area	of a parallelogram.
		recourse in a decire on y	Times a rais that gives the area	or a paramorogramm



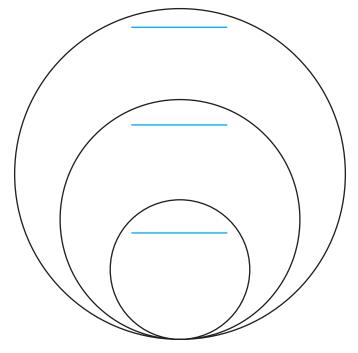
20.	Reason Abstractly If you were to draw three different parallelograms
	each with a base of 6 units and a height of 4 units, how would the areas
	compare?

21.	inquiry	HOW does finding the area of a parallelogram relate to finding the area of a rectangle?

## **Vocabulary Start-Up**

A polygon is a closed figure formed by 3 or more straight lines.

A parallelogram is a quadrilateral with opposite sides parallel and opposite sides the same length. A rhombus is a parallelogram with four equal sides. Fill in the lines in the diagram with polygon, parallelogram, or rhombus and draw an example of each.



## Real-World Link

**Stairs** Expert skateboarders can slide down the railings of stairs safely. A parallelogram is used to build a staircase. How many sets of parallel lines are shown in the parallelogram to the right?

### **Essential Question**

HOW does measurement help you solve problems in everyday life?



### Vocabulary

polygon parallelogram rhombus base height

formula

## COPS Common Core GPS

Content Standards
MCC6.G.1

Mathematical Practices 1, 3, 4, 7



## Key Concept

## Area of a Parallelogram



Work Zone

Words The area A of a parallelogram is the product of its base b and its height h.

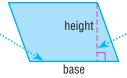
Model



**Symbols** A = bh

The area of a parallelogram is related to the area of a rectangle as you discovered in the previous Inquiry Lab.

The **base** of a parallelogram can be any one of its sides.



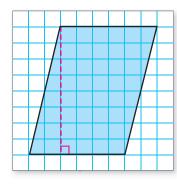
The **height** is the perpendicular distance from the base to the opposite side.

Parallelograms include special quadrilaterals, such as rectangles, squares, and rhombi.

## **Examples**



1. Find the area of the parallelogram.



The base is 6 units, and the height is 8 units.

A = bh

Area of parallelogram

 $A = 6 \cdot 8$ 

Replace b with 6 and h with 8.

A = 48

Multiply.

The area is 48 square units or 48 units<sup>2</sup>.

### can be written using abbreviations and an exponent of 2. For example: square units = units2

**Area Measurement** An area measurement

$$caucara units = units^2$$

$$square feet = ft^2$$

$$square\ meters = m^2$$

### 2. Find the area of the parallelogram.



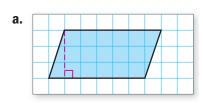
$$A = bh$$
 Area of parallelogram

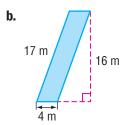
$$A = 20 \cdot 11$$
 Replace b with 20 and h with 11.

$$A = 220$$
 Check for Reasonableness  $220 \approx 200$   $\checkmark$ 

The area is 220 square centimeters or 220 cm<sup>2</sup>.

#### Got It? Do these problems to find out.







## Find Missing Dimensions

A formula is an equation that shows a relationship among certain quantities. To find missing dimensions, use the formula for the area of a parallelogram. Replace the variables with the known measurements. Then solve the equation for the remaining variable.

## **Example**



### **3.** Find the missing dimension of the parallelogram.

$$A = bh$$

Area of a parallelogram

$$45 = 9 \cdot h$$

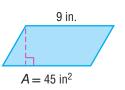
Replace A with 45 and b with 9.

$$\frac{45}{9} = \frac{9 \cdot h}{9}$$

Divide each side by 9.

$$5 = h$$

Simplify.



### So, the height is 5 inches.

### **Checking Your Work**

To check your work, replace b and h in the formula with 9 and 5.

$$A = bh$$

$$A = 9 \cdot 5$$

$$A = 45$$

Got It? Do these problems to find out.

d.

$$A = 48 \text{ m}^2$$

$$A = 96 \text{ yd}^2$$



### Height of **Parallelograms**

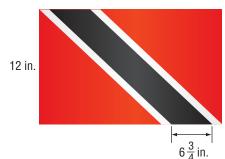
For the parallelogram formed by the area shaded black in Example 4, its height, 12 inches, is labeled outside the parallelogram.



### **Example**

4. Romilla is painting a replica of the national flag of **Trinidad and Tobago for a** research project. Find the area of the black stripe.

> The black stripe is shaped like a parallelogram. So, use the formula A = bh.



$$A = bh$$

Area of parallelogram

$$A = 6\frac{3}{4} \cdot 12$$

 $A = 6\frac{3}{4} \cdot 12$  Replace *b* with  $6\frac{3}{4}$  and *h* with 12. A = 81  $6\frac{3}{4} \cdot 12 = \frac{27}{4} \cdot 12$ , or 81

$$A = 81$$

$$6\frac{3}{4} \cdot 12 = \frac{27}{4} \cdot 12$$
, or 8

The area of the flag that is black is 81 square inches.

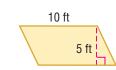
## **Guided Practice**



Find the area of each parallelogram. (Examples 1 and 2)

1.



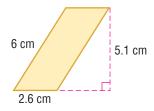




4. Find the height of a parallelogram if its base is 35 centimeters and its area is 700 square centimeters.

(Example 3)

**5.** The size of the parallelogram piece in a set of tangrams is shown at the right. Find the area of the piece. (Example 4)



Building on the Essential Question How are parallelograms related to triangles and rectangles?

Rate Yourself! How confident are you about the area of parallelograms? Shade the ring on the target. ľm Ineed help For more help, go online to access a Personal Tutor. FOLDABLES Time to update your Foldable!

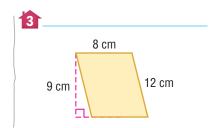
## Independent Practice

Find the area of each parallelogram. (Examples 1 and 2)

1.



**2.** base, 6 millimeters; height, 4 millimeters



4. Find the base of a parallelogram with an area of 24 square feet and

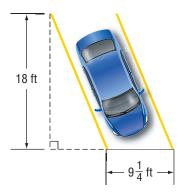
height 3 feet. (Example 3)

**5.** Find the area of the parking space shown to the right.

(Example 4)

**6.** STEM An architect designed three different parallelogram-shaped brick patios. Write the missing dimensions in the table.

Patio	Base (ft)	Height (ft)	Area (ft <sup>2</sup> )
1	$15\frac{3}{4}$		147
2		$11\frac{1}{4}$	$140\frac{5}{8}$
3	$10\frac{1}{4}$		$151\frac{3}{16}$



Show Your Work.

The base of a building is shaped like a parallelogram. The first floor has an area of 20,000 square feet. If the base of this parallelogram is 250 feet, can its height be 70 feet? Explain.

8. Colored Identify Structure Draw and label a parallelogram with a base twice as long as the height and an area less than 60 square inches. Find the area.

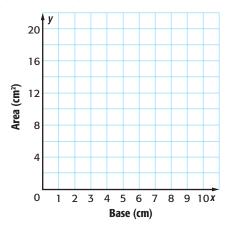
**9.** Multiple Representations Draw five parallelograms that each have a height of 4 centimeters and different base measurements on centimeter grid paper.



**a. Table** Make a table with a column for base, height, and area.

Base (cm)	Height (cm)	Area (cm <sup>2</sup> )	Ô
	4		
	4		
	4		
	4		
	4		

**b. Graph** Graph the ordered pairs (base, area).



c. Words Describe the graph. \_\_

# d

## H.O.T. Problems Higher Order Thinking

**10.** Persevere with Problems If x = 5 and y < x, which figure has the greater area? Explain your reasoning.





**11.** Reason Inductively Explain how the formula for the area of a parallelogram is related to the formula for the area of a rectangle.



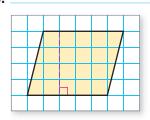
## **Georgia Test Practice**

- **12.** Robert used a piece of poster board shaped like a parallelogram to make a sign. The base of the poster board is 52 inches, and the area is 1,872 square inches. Find the height of the poster board.
  - A 884 in.
- © 42 in.
- B 176 in.
- ① 36 in.

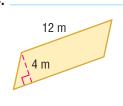
## **Extra Practice**

Find the area of each parallelogram.

13. 20 units2



14.



15. base, 12 inches; height, 15 inches

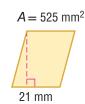
$$A = bh$$

$$A = 5 \cdot 4$$

$$A = 20$$

- **16.** Find the height of a parallelogram with base 6.75 meters and an area of 218.7 square meters.
- 17. Find the area of a parallelogram with base 15 yards and height  $21\frac{2}{3}$  yards.
- 18. What is the area of the region shown on the map?
  - 48.75 mi Ontario Seneca Yates 61.25 mi Steuben

19. What is the height of the parallelogramshaped pattern block shown below?



### Draw and label each figure. Then find the area.

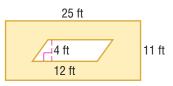
- **20.** a parallelogram with an equal base and height and an area greater than 64 square meters
- 21. a parallelogram with a base four times the height and an area less than 200 square feet



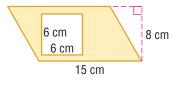


**MASS** Identify Structure Find the area of the shaded region in each figure.

22.

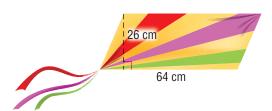


23.



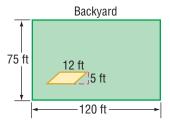
## **Georgia Test Practice**

**24.** The kite is in the shape of a parallelogram. What is the area of the kite shown below?



- A 8.32 cm<sup>2</sup>
- B 16.64 cm<sup>2</sup>
- © 832 cm<sup>2</sup>
- D 1,664 cm<sup>2</sup>

**25.** A family has a flower garden in the shape of a parallelogram in their backyard. They planted grass in the rest of the yard. What is the area of the backyard that is planted with grass?



- ⑤ 390 sq ft
- ⊕ 9,060 sq ft
- © 8,940 sq ft
- ① 9,144 sq ft
- **26. Short Response** A wallpaper design uses 15 parallelogram-shaped pieces of paper, each with a base of 3 inches and a height of 2 inches. How much paper is used to make the 15 pieces?



### **Common Core Review**

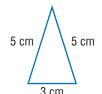
Draw each pair of lines. MCC4.G.1

27. parallel

28. intersecting

29. perpendicular

- **30.** Rosa has 22 songs in her music library. Michael has half as many. How many songs does Michael have in his music library? MCC4.NBT.6
- **31.** Name and describe the figure based on the lengths of its sides. MCC5.G.4



# **Inquiry Lab**

### **Area of Triangles**



HOW can you use the area of a parallelogram to find the area of a triangle?



Content Standards MCC6.G.1

Mathematical Practices 1, 3, 7, 8

Art Yurri is making a mosaic and is cutting rectangular tiles to make triangular tiles. He wants to find the area of the triangular tiles he is cutting.

What do you know?

What do you need to know? \_

## **Investigation 1**



Yurri starts with a rectangular piece that is 4 inches by 6 inches, similar to the size of an index card.

Step 1

Find the area of an index card.

 $A = \text{length} \times \text{width}$ 

inches × inches

square inches

4 in.



Step 2

Use an index card. Draw a diagonal line across your index card from one corner to another. Then cut across the line. Draw the resulting figures in the space below.



Step 3

Find the area of one of the remaining triangles. The triangle is exactly half the size of the related rectangle.

So, the area of the rectangle can be divided by 2 to find the area of one triangle.

÷ 2, or square inches. The area is

## Investigation 2

You can also find the area of a triangle from the area of a related parallelogram.

Step 1

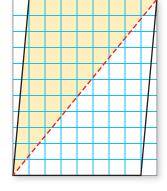
Copy the parallelogram shown on grid paper.

Step 2

Draw a diagonal as shown by the dashed line. Cut out the parallelogram. The area of the parallelogram is square units.

Step 3

Cut along the diagonal to form two triangles. Then find the area of one triangle. The triangle is half the size of the parallelogram. So, the area of the parallelogram can be divided by 2 to find the area of one triangle.

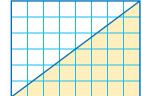


The area of one triangle is  $\div 2$  or square units.

# Collaborate

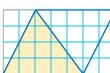
Work with a partner to find the area of each shaded triangle.

1.



length: \_\_\_\_\_

width: \_\_\_\_



base: \_\_\_\_

height: \_\_\_\_

area: \_\_\_\_\_ × \_\_\_\_ = \_\_\_\_

area of triangle = \_\_\_\_\_ square units



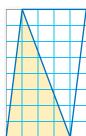
area of triangle = \_\_\_\_\_ square units

3.



length: \_\_\_\_\_

width: \_\_\_\_\_



base: \_\_\_\_\_

height:

area: \_\_\_\_\_ × \_\_\_\_ = \_\_

area of triangle = \_\_\_\_\_ square units

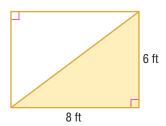
area: \_\_\_\_\_ × \_\_\_\_ = \_\_

area of triangle = \_\_\_\_\_ square units



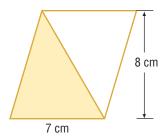
Work with a partner to find the area of each shaded triangle.

**5.** A = \_\_\_\_\_ square feet

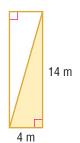




**7.** A = \_\_\_\_\_ square centimeters



**6.** A = \_\_\_\_\_ square meters

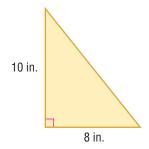


**8.** A =\_\_\_\_\_\_ square feet

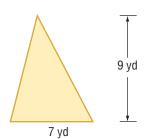


Identify Structure Draw dotted lines to show the parallelogram or rectangle that can be used to find the area of each triangle. Then find the area of each triangle.

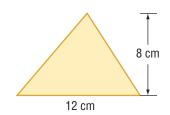
**9.** A =\_\_\_\_\_ square inches



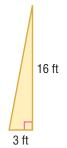
**10.** *A* = \_\_\_\_\_ square yards



**11.** A = \_\_\_\_\_ square centimeters



**12.** *A* = \_\_\_\_\_ square feet





The table shows the dimensions of several parallelograms. Use the area of each parallelogram to find the missing information for each triangle. Work with a partner to complete the table. The first one is already done for you.

	Parallelogram	Base, b	Height, h	Area of Parallelogram (units squared)	Triangle created with diagonal	Base, b	Height, <i>h</i>	Area of Each Triangle (units squared)
	Α	4	5	20	Α	4	5	10
13.	В	4	6		В	4		12
14.	С	2	5		С	2	5	
15.	D	3	4		D	3	4	
16.	Ε	6	3		Ε		3	9
17.	F	8	5		F	8	5	
18.	G	5	7		G	5		17.5
19.	Н	9	7		Н	9	7	
20.	I	11	5		I	11	5	

21.	Reason Inductively	How is the area of the parallelogram related to
	the area of a triangle with	the same base and height?

# Reflect

- 22. Identify Repeated Reasoning Write a formula that relates the area A of a triangle to the lengths of its base b and height h.
- HOW can you use the area of a parallelogram to find the area of a triangle?

## **Real-World Link**



**Biosphere** The Biosphere 2 complex in Tucson, Arizona, researches Earth and its living systems. Sections of the building are interlocking triangles of the same size.

1. There are two triangles that are outlined in the photo.

shape. They have the \_\_\_\_\_ size and the \_\_\_\_

2. Draw the figure formed by the two triangles.



- 3. How many small triangles make up the outlined parallelogram? How many small triangles make up each outlined triangle?
- 4. Describe the relationship between the area of one outlined triangle and the area of the outlined parallelogram.
- **5.** Draw another parallelogram like the one in the photo. Separate it into two triangles. Describe the relationship between the area of one triangle and the parallelogram.





### **Essential Question**

HOW does measurement help you solve problems in everyday life?



### Vocabulary

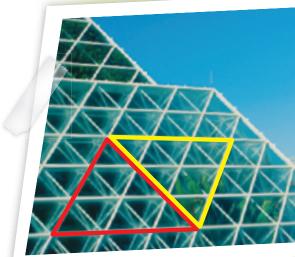
congruent



#### **Common Core GPS**

**Content Standards** MCC6.G.1

**Mathematical Practices** 1, 3, 4, 8



## Key Concept

## **Area of a Triangle**

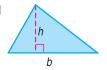
Work Zone

**Words** The area *A* of a triangle is one

half the product of the base b and its height h.

Symbols  $A = \frac{1}{2}bh$  or  $A = \frac{bh}{2}$ 

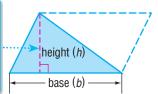
Model



Congruent figures are figures that are the same shape and size.

A parallelogram can be formed by two congruent triangles. Since congruent triangles have the same area, the area of a triangle is one half the area of the parallelogram.

The base of a triangle can be any one of its sides. The height is the perpendicular distance from that base to the opposite vertex.

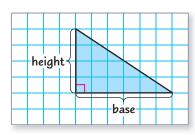


## **Examples**





1. Find the area of the triangle.



By counting, you find that the measure of the base is 6 units and the height is 4 units.

$$A = \frac{1}{2}bh$$
 Area of a triangle

$$A = \frac{1}{2}(6)(4)$$
 Replace b with 6 and h with 4.

Multiply.

$$A = \frac{1}{2}(24)$$
 Multiply.

A = 12

You can use mental math to multiply  $\frac{1}{2}$ (6)(4). Think: Half of 6 is 3, and 3  $\times$  4 is 12.

### 2. Find the area of the triangle.



Area of a triangle

$$A = \frac{1}{2}(12.1)(6.4)$$

Replace b with 12.1

$$A = \frac{1}{2}(77.44)$$

Multiply.

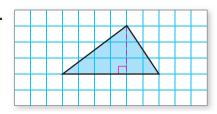
$$A = 38.72$$

Divide.  $\frac{1}{2}$ (77.44) = 77.44 ÷ 2, or 38.72

The area of the triangle is 38.72 square meters.

#### Got It? Do these problems to find out.







12.1 m

6.4 m



## **Find Missing Dimensions**

Use the formula for the area of a triangle to find missing dimensions.

## **Example**



### **3.** Find the missing dimension of the triangle.

$$A = \frac{bh}{2}$$

Area of a triangle

$$24 = \frac{b \cdot 6}{2}$$

Replace A with 24 and



$$48 = b \cdot 6$$

$$\frac{48}{6} = \frac{b \cdot 6}{6}$$

Simplify.

$$\frac{48}{6} = \frac{b \cdot 6}{6}$$

Divide each side by 6.

$$8 = b$$

Simplify.

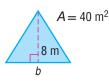


### **Check for** Reasonableness

To check your work, replace band hwith the measurements and solve to find the area.

#### Got It? Do these problems to find out.

C.



d.

$$A = 72 \text{ yd}^2$$

6 cm

b  $A = 24 \text{ cm}^2$ 



4. The front of a camping tent has the dimensions shown. How much material was used to make the front of the tent?



Area of a triangle

$$A = \frac{1}{2}(5)(3)$$

Replace b with 5 and

$$A = \frac{1}{2}(15)$$
 or 7.5

Multiply.

The front of the tent has an area of 7.5 square feet.

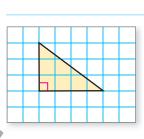


## **Guided Practice**

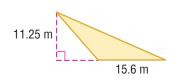


Find the area of each triangle. (Examples 1 and 2)

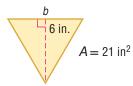
1.



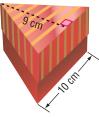




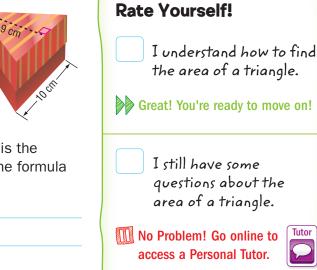
4. Tayshan designs uniquely shaped ceramic floor tiles. What is the base of the tile shown? (Example 3)



**5.** Consuela made a triangular paper box as shown. What is the area of the top of the box? (Example 4)



6. **Q** Building on the Essential Question How is the formula for the area of a triangle related to the formula for the area of a parallelogram?



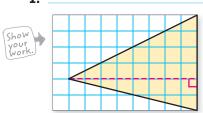
FOLDABLES Time to update your Foldable!

## Independent Practice

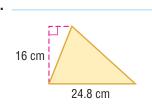


Find the area of each triangle. (Examples 1 and 2)

1.



2.



3

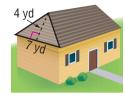


Find the missing dimension of each triangle described. (Example 3)

**4.** height: 14 in. area: 245 in<sup>2</sup>

**5.** base: 27 cm area: 256.5 cm<sup>2</sup>

**6.** Ansley is going to help his father shingle the roof of their house. What is the area of the triangular portion of one end of the roof? (Example 4)



- Multiple Representations The table shows the areas of a triangle where the base of the triangle stays the same but the height changes.
  - **a. Algebra** Write an algebraic expression that can be used to find the area of a triangle that has a base of 5 units and a height of *n* units.
  - **b. Graph** Graph the ordered pairs (height, area).

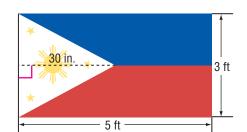
	y			Т							
30	_										
27-											
30 27 24											
21											
18											
15											
12				-							
9											
6											
-3											
4	<u> </u>				4			7 (			O *
0	,	1	2	3	4	5 (	6 7	( )	3 9	9 1	0 <b>x</b>

c. Words Describe the graph.

Area of Triangles									
Base (units)	Area (units <sup>2</sup> )								
5	2	5							
5	4	10							
5	6	15							
5	8	20							
5	n	?							

8. What is the area of the triangle on the flag of the

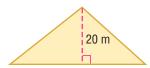
Philippines in inches?

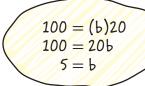




### H.O.T. Problems Higher Order Thinking

9. Find the Error Dwayne is finding the base of the triangle shown. Its area is 100 square meters. Find his mistake and correct it.







**10.** Persevere with Problems How can you use triangles to find the area of the hexagon shown? Draw a diagram to support your answer.

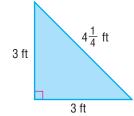


11. Identify Repeated Reasoning Draw a triangle and label its base and height. Draw another triangle that has the same base, but a height twice that of the first triangle. Find the area of each triangle. Then write a ratio that expresses the area of the first triangle to the area of the second triangle.



## **Georgia Test Practice**

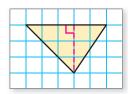
- **12.** A piece of metal is cut in the shape of the triangle below. What is the area of the piece of metal?
  - $\bigcirc$   $3\frac{1}{4}$  ft<sup>2</sup>
  - (B)  $4\frac{1}{2}$  ft<sup>2</sup>
  - ©  $6\frac{3}{8}$  ft<sup>2</sup>
  - ① 9 ft<sup>2</sup>



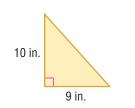
## **Extra Practice**

Find the area of each triangle.

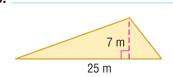
13.  $7\frac{1}{2}$  units<sup>2</sup>



14.



**15**.



Homework Help

$$A = \frac{bh}{2}$$

$$A = \frac{5 \cdot 3}{2}$$

$$A = \frac{15}{2} \text{ or } 7\frac{1}{2}$$

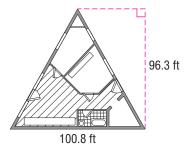
Find the missing dimension of each triangle described.

**16.** height: 7 in., area: 21 in<sup>2</sup>

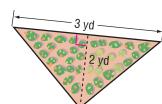
**17.** base: 11 m, area: 115.5 m<sup>2</sup>

**18.** base: 14.2 yd, area: 63.9 yd<sup>2</sup>

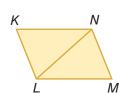
- **19.** height: 11 cm, area: 260.15 cm<sup>2</sup>
- **20.** STEM An architect is designing a building on a triangular plot of land. If the base of the triangle is 100.8 feet and the height is 96.3 feet, find the available floor area of the building.



- 21. A flower bed in a parking lot is shaped like a triangle as shown.
  - **a.** Find the area of the flower bed in square feet.
  - **b.** If one bag of topsoil covers 10 square feet, how many bags are needed to cover this flower bed?



**22. Identify Repeated Reasoning** Refer to parallelogram *KLMN* at the right. If the area of parallelogram *KLMN* is 35 square inches, what is the area of triangle *KLN*?



## **Georgia Test Practice**

**23.** The table shows the areas of a triangle where the height of the triangle stays the same but the base changes.

Areas of Triangles						
Height (units)	Base (units)	Area (square units)				
7	2	7				
7	3	$10\frac{1}{2}$				
7	4	14				
7	5	$17\frac{1}{2}$				
7	х	?				

Which expression can be used to find the area of a triangle that has a height of 7 units and a base of *x* units?

- A 7x
- ©  $\frac{7}{2}$
- $\bigcirc \frac{x}{2}$

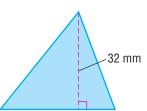
- 24. Norma cut a triangle out of construction paper for an art project.

  The area of the triangle hcm is 84.5 square centimeters. What is the height of the triangle?
  - € 6.5 cm
- ⊕ 26 cm

13 cm

- © 13 cm
- ① 169 cm
- **25. Short Response** The triangle has an area of 640 square millimeters. What is the

base of the triangle?

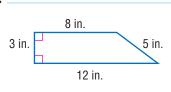




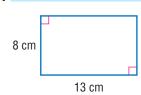
### **Common Core Review**

Identify each figure below as a rectangle, rhombus, or trapezoid. MCC5.G.4

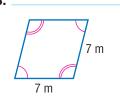
26.



27.



28.

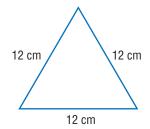


**29.** Jackson's floor rug has four 90° angles. All four sides are 18 inches long. The rug has two sets of parallel sides. What shape is Jackson's floor rug?

MCC5.G.4

30. How many lines of symmetry can be drawn for the figure shown?

Draw them on the figure. Mcc4.G.3



# **Inquiry Lab**

### Area of Trapezoids



HOW can you use the area of a parallelogram to find the area of a corresponding trapezoid?

Content Standards MCC6.G.1

Mathematical **Practices** 

1, 3, 5, 7

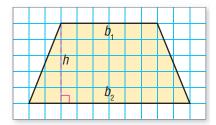
**Garden** Lizette is building a garden in the shape of a trapezoid. The garden is 6 feet wide in the back, 10 feet wide in the front, and 5 feet from back to front. She wants to find the area of the garden.

## Investigation 1

Find the area of a trapezoid by drawing the related parallelogram.

Step 1 Trace the trapezoid below on grid paper. Label the height h and label the bases  $b_1$  and  $b_2$ .

> A trapezoid has two bases, b<sub>1</sub> and  $b_2$ . The height h of a trapezoid is the perpendicular distance between the bases.

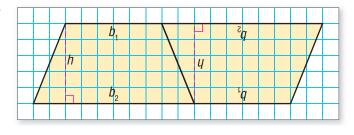


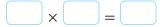
The shorter base  $b_1$  represents the garden width of

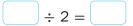
The longer base  $b_2$  represents the garden width of

The height h represents the garden dimension of \_

- Step 2 Cut out another trapezoid that is identical to the one in Step 1.
- Step 3 Tape the trapezoids together as shown.
- Step 4 Find the area of the parallelogram. Then divide by 2 to find the area of each trapezoid.







So, the area of the garden is square feet.

connectED.mcgraw-hill.com

## Investigation 2



Discover the formula for the area of a trapezoid.

Step 1 What figure is formed by the two trapezoids in

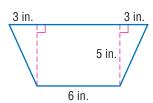
Investigation 1?

Write an addition expression to represent the length of the base of the entire figure.

- **Step 2** Write a formula for the area A of the parallelogram using  $b_1$ ,  $b_2$ , and h.
- Step 3 How does the area of each trapezoid compare to the area of the parallelogram?
- **Step 4** Write a formula for the area A of each trapezoid using  $b_1$ ,  $b_2$ , and h.

## Investigation 3

Another way to find the area of a trapezoid is to deconstruct it to determine which figures form the trapezoid. Find the area of the trapezoid shown below.



Step 1 The trapezoid is made up of one rectangle and two congruent triangles. Find the area of the shapes that make up the trapezoid.

The area of the rectangle is  $\times$  = square inches.

The area of each triangle is  $\frac{\times}{}$  =  $\frac{\times}{}$  square inches.

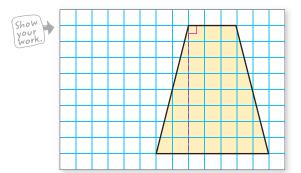
Step 2 Add the areas.

+ + square inches



# Use Math Tools Work with a partner. Find the area of each trapezoid by drawing the related parallelogram.

**1.** A =\_\_\_\_\_ square units



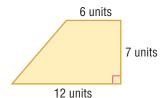
**2.** A = \_\_\_\_\_ square units



### Work with a partner. Find the area of each trapezoid by using the formula.

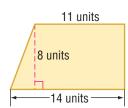
**3.** 
$$A = \frac{( + ) ( + )$$

A = \_\_\_\_\_ square units



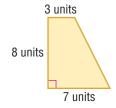
**4.** 
$$A = \frac{( + )}{( + )}$$

A = \_\_\_\_\_ square units

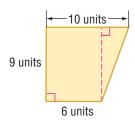


### Work with a partner. Decompose each trapezoid to find the area.

**5.** 
$$A =$$
 \_\_\_\_\_ square units



**6.** 
$$A =$$
 \_\_\_\_\_ square units





The table shows the dimensions of several parallelograms and corresponding trapezoids. Work with a partner to complete the table. The first one is done for you.

	Dimensions of Parallelogram	Area of Parallelogram	Length of Trapezoid $b_1$	Length of Trapezoid $b_2$	Trapezoid Height	Area of Trapezoid	
	7	28	2	5	4	14	
7.	6		5	6	6	J	
8.	5 12		8	4	5		
9.	b = 11 $b = 3$		7	4	3		

- **10.** Reason Inductively Compare the dimensions of the parallelogram to the dimensions of the corresponding trapezoid. What pattern do you see in the table?
- 11. Reason Inductively Compare the area of the parallelogram to the area of the corresponding trapezoid. What pattern do you see in the table?

# Reflect

- **12.** Write the formula for the area A of a trapezoid with bases  $b_1$  and  $b_2$  and height h.
- HOW can you use the area of a parallelogram to find the area of a corresponding trapezoid?



### **Essential Question**

HOW does measurement help you solve problems in everyday life?



### **Common Core GPS**

**Content Standards** MCC6.G.1

Mathematical Practices

1, 2, 3, 4, 7, 8



## **Real-World Link**

Window Seat Kiana has a bay window in her room. The window seat is in the shape of a trapezoid. She needs to measure the seat in order to sew a cushion for the seat. The blue trapezoid in the diagram below represents the dimensions of the window seat.

Use the diagram below to describe the relationship between trapezoids and rectangles.

Find the dimensions of each figure.

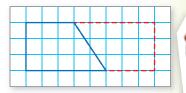
**Trapezoid** Rectangle

units

base 1: units length: units base 2:

height:

height: units



2. What is the relationship between the measures of the rectangle and the measures of the trapezoid?

units

3. Make a Conjecture How is the area of a trapezoid related to the area of a rectangle?



## Key Concept

## **Area of a Trapezoid**



Work Zone

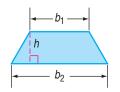
**Words** The area A of a trapezoid is one

half the product of the height h and the sum of the bases  $b_1$ 

and  $b_2$ .

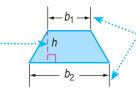
**Symbols**  $A = \frac{1}{2}h(b_1 + b_2)$ 

Model



A trapezoid has two bases,  $b_1$  and  $b_2$ . The height of a trapezoid is the distance between the bases.

The height is the perpendicular distance between the bases.



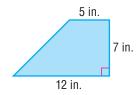
The two bases are parallel. They will always be the same distance apart.

When finding the area of a trapezoid, it is important to follow the order of operations. In the formula, the bases are to be added before multiplying by  $\frac{1}{2}$  of the height h.

## **Examples**



1. Find the area of the trapezoid.



The bases are 5 inches and 12 inches.

The height is 7 inches.

$$A = \frac{1}{2} h(b_1 + b_2)$$
 Area of a trapezoid

$$A = \frac{1}{2}$$
(7)(5 + 12) Replace *h* with 7, *b*<sub>1</sub> with 5, and *b*<sub>2</sub> with 12.

$$A = \frac{1}{2}(7)(17)$$
 Add 5 and 12.

$$A = 59.5$$
 Multiply.

The area of the trapezoid is 59.5 square inches.

2. Find the area of the trapezoid.

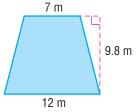
$$A = \frac{1}{2}h(b_1 + b_2)$$

Area of a trapezoid

$$A = \frac{1}{2}(9.8)(7 + 12)$$

Replace h with 9.8,

 $b_1$  with 7, and  $b_2$  with 12.



$$A = \frac{1}{2}(9.8)(19)$$

Add 7 and 12.

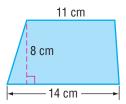
$$A = 93.1$$

Multiply.

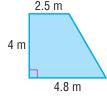
So, the area of the trapezoid is 93.1 square meters.

#### Got It? Do these problems to find out.

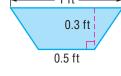




b.



h



12 ft

15 ft

## Find the Missing Height

Use the related formula,  $h = \frac{2A}{b_1 + b_2}$ , to find the height of a trapezoid.

#### **Example**



3. The trapezoid has an area of 108 square feet. Find the height.

$$h = \frac{2A}{b_1 + b_2}$$

Height of a trapezoid

$$h = \frac{2(108)}{12 + 15}$$

Replace A with 108, b<sub>1</sub> with 12, and  $b_2$  with 15.

$$h = \frac{216}{27}$$

Multiply 2 and 108. Add 12 and 15.

Divide.

So, the height of the trapezoid is 8 feet.

#### **Be Precise**

Check your answer by using the formula for the area of a trapezoid.

#### Got It? Do these problems to find out.

**d.** 
$$A = 24 \text{ cm}^2$$

$$b_1 = 4 \text{ cm}$$

$$b_2 = 12 \text{ cm}$$
  
 $h = ?$ 

$$h = ?$$

**e.** 
$$A = 21 \text{ yd}^2$$

$$b_1 = 2 \text{ yd}$$

$$b_2 = 5 \text{ yd}$$
  
 $h = ?$ 



#### Mental Math

To multiply  $\frac{1}{2}(51)(64)$ , it is easier to use the Commutative Property to reorder the factors as  $\frac{1}{2}$ (64)(51) and take half of 64 instead of half of 51.



#### **Example**



4. The shape of Osceola County, Florida, resembles a trapezoid. Find the approximate area of this county.

Florida, resembles a trapezoid.

Find the approximate area of this county.

$$A = \frac{1}{2}h(b_1 + b_2)$$

$$A = \frac{1}{2}(51)(48 + 16)$$

$$A = \frac{1}{2}(51)(64)$$

$$A = \frac{1}{2}(51)(64)$$
Add 48 and 16.

A = 1,632

Multiply.

So, the approximate area of the county is

Area of a trapezoid Replace h with 51, b<sub>1</sub> with 48, and b<sub>2</sub> with 16.

Add 48 and 16.

Multiply.

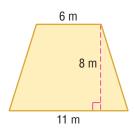
So, the approximate area of the county is 1,632 square miles.

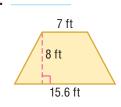
# **Guided Practice**



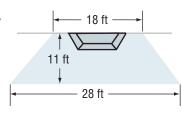
Find the area of each trapezoid. Round to the nearest tenth if necessary. (Examples 1 and 2)

1.



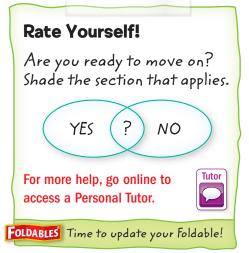


- 3. A trapezoid has an area of 15 square feet. If the bases are 4 feet and 6 feet, what is the height of the trapezoid? (Example 3)
- 4. In the National Hockey League, goaltenders can play the puck behind the goal line only in a trapezoid-shaped area, as shown at the right. Find the



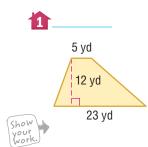
area of the trapezoid. (Example 4)

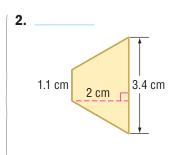
**Building on the Essential Question** How is the formula for the area of a trapezoid related to the formula for the area of a parallelogram?

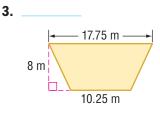


## Independent Practice

Find the area of each trapezoid. Round to the nearest tenth if necessary. (Examples 1 and 2)

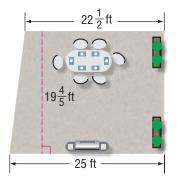




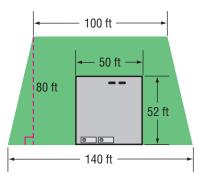


- **4.** A trapezoid has an area of 150 square meters. If the bases are 14 meters and 16 meters, what is the height of the trapezoid?

  (Example 3)
- **5.** A trapezoid has an area of 400 square millimeters. The bases are 14 millimeters and 36 millimeters. What is the height of the trapezoid? (Example 3)
- **6.** Find the area of the patio shown. (Example 4)



- \*\*Use the diagram that shows the lawn that surrounds an office building.
  - **a.** What is the area of the lawn?
  - **b.** If one bag of grass seed covers 2,000 square feet, how many bags are needed to seed the lawn?



8. Reason Abstractly Tiles are being placed in front of a fireplace to create a trapezoidal hearth. The hearth will have a height of 24 inches and bases that are 48 inches and 60 inches. If the tiles cover 16 square inches, how many tiles will be needed?

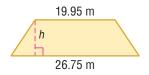
- **9.** a trapezoid with no right angles and an area less than 12 square centimeters
- **10.** a trapezoid with a right angle and an area greater than 40 square inches





#### H.O.T. Problems Higher Order Thinking

**11.** Persevere with Problems Apply what you know about rounding to explain how to estimate the height h of the trapezoid shown if the area is  $235.5 \text{ m}^2$ .



12. Identify Repeated Reasoning Find two possible lengths of the bases of a trapezoid with a height of 1 foot and an area of 9 square

feet. Explain how you found your answer.



#### **Georgia Test Practice**

**13.** Barrington cuts a piece of wood in the shape of a trapezoid. The height is 4 feet. The top is 3 feet across and the bottom is 10 feet across. Which equation could be used to find the area of the piece of wood?

(A) 
$$10 = \frac{1}{2} \times h(4 + 3)$$

(B) 
$$A = \frac{1}{2} \times 10(4 + 3)$$

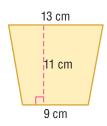
$$\bigcirc$$
  $A = \frac{1}{2} \times 3(4 + 10)$ 

① 
$$A = \frac{1}{2} \times 4(3 + 10)$$

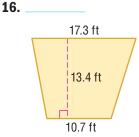
#### **Extra Practice**

Find the area of each figure. Round to the nearest tenth if necessary.

14. 121 cm<sup>2</sup>



23 ft



Homework Help

$$A = \frac{1}{2}\lambda(b_1 + b_2)$$

$$A = \frac{1}{2}(11)(13 + 9)$$

$$A = \frac{1}{2}(11)(22)$$

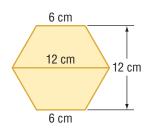
$$A = 121$$

- **17.** A trapezoid has an area of 50 square inches. The bases are 3 inches and 7 inches. What is the height of the trapezoid?
- **18.** A trapezoid has an area of 18 square miles. The bases are 5 miles and 7 miles. What is the height of the trapezoid?
- **19.** A county is shaped like a trapezoid. Its northern border is about 9.6 miles across, and the southern border is approximately 25 miles across. The distance from the southern border to the northern border is about 90 miles. Find the approximate area of the county.
- **20.** A play tent is shown. How much fabric was used to make the front and back of the play tent?

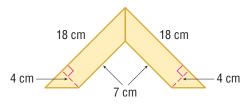


Identify Structure Each figure below is made up of congruent trapezoids. Find the area of each figure.

21.



22.



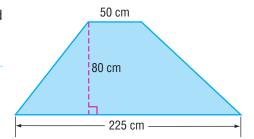
## **Georgia Test Practice**

- 23. Find the area of a trapezoid with a height of 4 yards and bases of  $5\frac{1}{2}$  yards and  $6\frac{1}{2}$  yards.
  - A 16 square yards
  - ® 24 square yards
  - ©  $28\frac{1}{2}$  square yards
  - 143 square yards

24. Short Response Serina designed the bag shown. How much fabric will be needed to make the front of the bag?



25. Short Response A piece of sod is shaped like a trapezoid as shown. What is the area of the piece of sod?



#### **Common Core Review**

Add or multiply. MCC5.NBT.7

**26.** 
$$5 + 6.2 + 8.8 =$$
 **27.**  $8 \times 8 \times 4 =$  **27.**  $8 \times 8 \times 4 =$  **28.**  $8 \times 8 \times 4 =$  **29.**  $8 \times 8 \times 4 =$  

**27.** 
$$8 \times 8 \times 4 =$$

29. Find the perimeter of the rectangle. MCC4.MD.3



**30.** Delanie is building a rectangular frame for her favorite photograph. The frame is 7 inches wide and 5 inches long. What is the perimeter

of the frame? MCC4.MD.3

What are the dimensions of the rectangle?



#### Understand What are the facts?

Twelve tiles will be arranged with the least perimeter possible.



#### Plan What is your strategy to solve this problem?

Use graph paper. Make diagrams of 12 squares to represent 12 tiles.



Solve How can you apply the strategy?

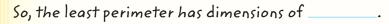
A rectangle with dimensions of 12 and 1 has a perimeter of

A rectangle with dimensions of 3 and 4

has a perimeter of

A rectangle with dimensions of 2 and 6

has a perimeter of





#### **Check** Does the answer make sense?

Use addition to check your answer.

$$3+4+3+4=14$$
  $2+6+2+6=16$   $12+1+12+1=26$ 





Identify Structure Describe a design with a perimeter and an area of 16.

Case #2 Dynamic Dimensions

For a school assignment, Santiago has to give three different possibilities for the dimensions of a rectangle that has a perimeter of 28 feet and an area greater than 30 square feet. One of the diagrams he drew is shown at the right.

What are two other possibilities for the dimensions of the rectangle?





#### Understand

Read the problem. What are you being asked to find?

I need to find

Underline key words and values in the problem. What information do you know?

The perimeter of the rectangle is feet, and the area is greater than \_\_\_\_

#### Plan

Choose a problem-solving strategy.

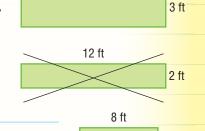
I will use the strategy.

#### Solve

Use your problem-solving strategy to solve the problem.

Draw rectangles with perimeters of Then, multiply length times width to find the area.

The product must be greater than



11 ft

So, the dimensions of two possible rectangles are



#### Check

Use information from the problem to check your answer.

Reread the problem. Check that both conditions have been met.

> 30 and Perimeter: = 28Area: > 30 6 ft



**Collaborate** Work with a small group to solve the following cases. Show your work on a separate piece of paper.

#### Case #3 Decorations

A rectangular table that is placed lengthwise against a wall is 8 feet long and 3 feet wide. Balloons will be attached 1 foot apart along the three exposed sides, with one balloon at each of the four corners.

How many balloons are needed?



## Case #4 Geography

The mall is 10 miles from your home. Your school is one half of the way from your home to the mall. The library is two fifths of the way from your

How many miles is it from your home to the library?

#### Case #5 Painting

Van is going to paint a mural in his home. The mural is in the shape of a parallelogram with a base of 8 feet and a height of 15 feet.

- a. What is the area of the mural?
- b. If one quart of paint will cover 70 square feet, how many quarts of paint does Van need to buy?

#### Circle a strategy below to solve the problem. · Look for a pattern. · Work backward.

· Guess, check, and revise. · Make a table.

#### Case #6 Geometry

The base and height of each successive triangle are each half the length of the previous triangle.

16 cm

What will be the area of the fourth triangle?

# Mid-Chapter Check

#### Vocabulary Check



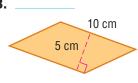
- 1. Be Precise Define polygon. Give an example of a figure that is a polygon and an example of a figure that is not a polygon. (Lesson 1)
- 2. Fill in the blank in the sentence below with the correct term(s). (Lesson 2)

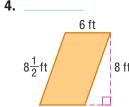
Congruent figures have the \_ size and the shape.

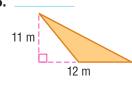
#### Skills Check and Problem Solving

Find the area of each figure. (Lessons 1 and 2)

3.



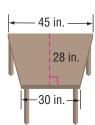




Find the missing dimension of each figure. (Lessons 1 and 3)

- **6.** parallelogram:  $h = 5\frac{1}{4}$  ft; A = 12 ft<sup>2</sup>
- 7. trapezoid:  $b_1 = 3 \text{ m}$ ;  $b_2 = 4 \text{ m}$ ;  $A = 7 \text{ m}^2$

8. Model with Mathematics A corner table is in the shape of a trapezoid. Find the area of the tabletop. (Lesson 3)



- 9. Georgia Test Practice What is the height of a triangle with a base of 14 centimeters and an area of 56 square centimeters? (Lesson 2)
  - A 112 centimeters
- © 8 centimeters
- B 56 centimeters
- 7 centimeters

HOW does measurement help you solve problems in everyday life?



**Common Core GPS** 

**Content Standards** MCC6.G.1

**Mathematical Practices** 1, 2, 3, 4, 7

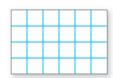


#### **Real-World Link**

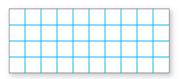
Construction Mr. Blackwell is building a rectangular dog house. The floor of the dog house is 4 feet long and 2 feet wide.

1. Draw the floor of the dog house on the graph paper below.





- 2. Add the lengths of the sides to find the perimeter.
- 3. Multiply the length and width to find the area.
- 4. Mr. Blackwell doubles the width of the dog house. Draw the new floor below.



5. How did the perimeter and area of the floors change from the first to the second dog house?





## Key Concept

#### **Changing Dimensions: Effect on Perimeter**

Work Zone

**Words** If the dimensions of a polygon are multiplied by x, then the perimeter of the polygon changes by a factor of x.

Model



**Example** The dimensions of Figure A are multiplied by 2 to produce Figure B.

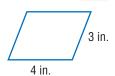
perimeter of Figure A 
$$\cdot$$
 2 = perimeter of Figure B  $\cdot$  2 = 16

Notice that all the dimensions of the figure must change using the same factor,  $\boldsymbol{x}$ .

#### **Example**



 Suppose the side lengths of the parallelogram at the right are tripled. What effect would this have on the perimeter? Justify your answer.

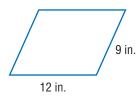


The dimensions are 3 times greater.

original perimeter: 2(4) + 2(3) = 14 in.

new perimeter: 2(12) + 2(9) = 42 in.

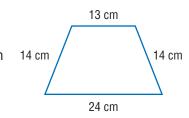
compare perimeters: 42 in.  $\div$  14 in. = 3



So, the perimeter is 3 times the perimeter of the original figure.

Got It? Do this problem to find out.

**a.** Suppose the side lengths of the trapezoid at the right are multiplied by  $\frac{1}{2}$ . What effect would this have on the perimeter? Justify your answer.



a.\_

## **Changing Dimensions: Effect on Area**

Key Concept

Words

If the dimensions of a polygon are multiplied by x, then the area of the polygon changes by  $x \cdot x$  or  $x^2$ .

Model



Figure B

10

**Example** 

The dimensions of Figure A are multiplied by 2 to produce Figure B.

area of Figure A • 
$$2^2$$
 = area of Figure B •  $4$  = 80

Notice that all the dimensions of the figure must change using the same factor, x.

#### **Example**

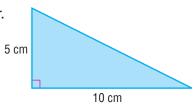


2. The side lengths of the triangle at the right are multiplied by 5. What effect would this have on the area? Justify your answer.



The dimensions are 5 times greater.

original area: 
$$\frac{1}{2} \cdot 2 \cdot 1 = 1 \text{ cm}^2$$
  
new area:  $\frac{1}{2} \cdot 10 \cdot 5 = 25 \text{ cm}^2$ 



compare areas:

$$25 \text{ cm}^2 \div 1 \text{ cm}^2 = 25 \text{ or } 5^2.$$

So, the area is  $5^2$  or 25 times the area of the original figure.

#### Got It? Do this problem to find out.

**b.** A rectangle measures 2 feet by 4 feet. Suppose the side lengths are multiplied by 2.5. What effect would this have on the area? Justify your answer.



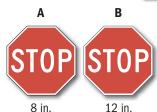
b. \_\_\_\_\_







**3.** A stop sign is in the shape of a regular octagon. Sign A shown at the right has an area of 309 square inches. What is the area of sign B?



Since  $8 \times 1.5 = 12$ , the area of sign B is  $1.5^2$  times the area of sign A.

$$309 \cdot 1.5^2 = 309 \cdot 2.25$$
 or  $695.25$ 

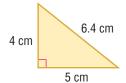
So, the area of sign B is 695.25 square inches.

#### **Guided Practice**



Refer to the figure at the right for Exercises 1 and 2. Justify your answers. (Examples 1-2)

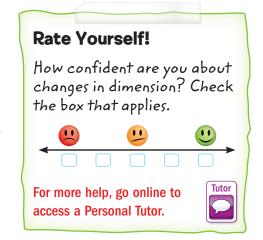
**1.** Each side length is doubled. Describe the change in the perimeter.



- 2. Each side length is tripled. Describe the change in the area.
- 3. Different sizes of regular hexagons are used in a quilt. Each small hexagon has side lengths of 4 inches and an area of 41.6 square inches. Each large hexagon has side lengths of 8 inches. What is the area of each

large hexagon? (Example 3) \_

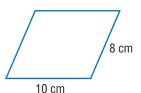
Building on the Essential Question How can exponents help you find the area of a rectangle if each side length is multiplied by x?



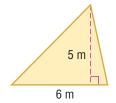
#### Independent Practice



Each side length of the parallelogram at the right is multiplied by 4. Describe the change in the perimeter. Justify your answer. (Example 1)



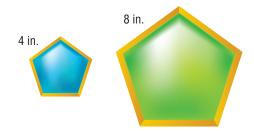
2. The base and height of the triangle at the right are multiplied by 4. Describe the change in the area. Justify your answer. (Example 2)



Each side length of the rectangle is multiplied by  $\frac{1}{3}$ . Describe the change in the area. Justify your answer. (Example 2)

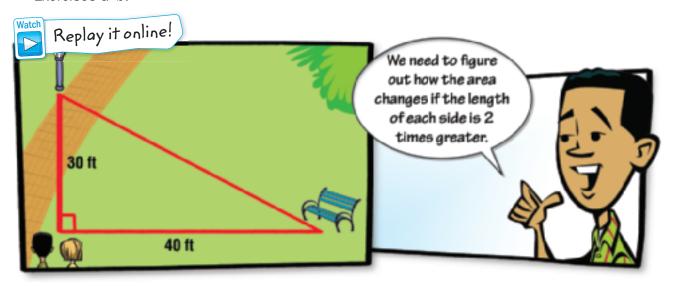


4. Different sizes of regular pentagons are used in a stained glass window. Each small pentagon has side lengths of 4 inches and an area of 27.5 square inches. Each large pentagon has side lengths of 8 inches. What is the area of each large pentagon? (Example 3)



5. Justify Conclusions A dollhouse has a bed with dimensions  $\frac{1}{12}$  the size of a queen-size bed. A queen-size bed has an area of 4,800 square inches, and a length of 80 inches. What are the side lengths of the dollhouse bed? Justify your answer.

**6.** Reason Abstractly Refer to the graphic novel frame below for Exercises a–b.



- a. What is the original area of the triangle?
- b. What is the new area if the sides are all two times longer?



#### H.O.T. Problems Higher Order Thinking

7. **Eldentify Structure** Sketch a triangle with the side lengths labeled. Sketch and label another triangle that has a perimeter two times greater than the perimeter of the first triangle.



**8.** Persevere with Problems The corresponding side lengths of two figures have a ratio of  $\frac{a}{b}$ . What is the ratio of the perimeters? the ratio of the areas?



#### **Georgia Test Practice**

- **9.** The regular pentagon shown at the right is enlarged so that its sides are four times longer. What effect does this have on the perimeter?
  - A The perimeter is 4 times greater.
  - B The perimeter is 12 times greater.
  - © The perimeter is 16 times greater.
  - ① The perimeter is 20 times greater.

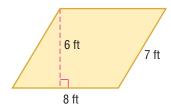


3 cm

#### **Extra Practice**

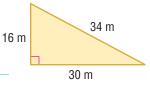
Refer to the parallelogram at the right for Exercises 10–12. Justify your answers.

**10.** Suppose the base and height are each multiplied by  $\frac{1}{2}$ . What effect would this have on the area?



Homework Help original area:  $8 \cdot 6$  or 48 square feet new dimensions: base  $= 8 \cdot \frac{1}{2}$  or 4 ft, height  $= 6 \cdot \frac{1}{2}$  or 3 ft new area:  $4 \cdot 3$  or 12 square feet; 12 ft<sup>2</sup>  $\div 48$  ft<sup>2</sup>  $= \frac{1}{4}$ ; So, the area is  $\frac{1}{2} \cdot \frac{1}{2}$  or  $\frac{1}{4}$  times the area of the original figure.

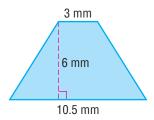
- **11.** Suppose the side lengths are multiplied by 6. Describe the change in the perimeter.
- **12.** Suppose the base and height are each multiplied by 3.5. Describe the change in the area.
- **13.** Refer to the triangle at the right. Suppose the side lengths and height of the triangle were divided by 4. What effect would this have on the perimeter? the area? Justify your answer.



14. Ustify Conclusions A model car has a windshield with dimensions  $\frac{1}{18}$  the size of a real car windshield. The rectangular windshield of the real car has an area of about 2,318 square inches, with a width of 61 inches. What are the side lengths of the model car's windshield? Round to the nearest hundredth. Justify your answer.

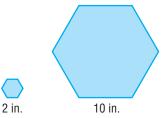
#### **Georgia Test Practice**

**15.** The lengths of the bases and height of the trapezoid below are doubled. How does the area of the trapezoid change?



- The area doubles.
- B The area triples.
- © The area is 4 times greater.
- The area is 6 times greater.
- **16. Short Response** Two regular pentagons have side lengths of 1 centimeter and 7 centimeters, respectively. How many times greater is the perimeter of the larger pentagon?

17. Two regular hexagons are shown below. How many times greater is the area of the larger hexagon than the smaller hexagon?



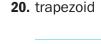
- F) 2 times
- H 10 times
- © 5 times
- 1 25 times
- **18.** Two equilateral triangles have perimeters of 9 meters and 27 meters, respectively. How many times greater is the area of the larger triangle?
  - A 2 times
- © 9 times
- 3 times
- © 27 times



#### **Common Core Review**

Describe the sides of each figure using the terms parallel, perpendicular, and congruent. MCC5.G.4

**19.** parallelogram





- 21. Mr. Macy's garden is surrounded by a fence. The fence makes four right angles at each corner. All four sides of the fence are 14 meters long. What shape best describes Mr. Macy's garden? MCC5.G.4
- 22. Gary drew the logo to the right. The blue figure has two pairs of parallel sides, two pairs of congruent sides, and four right angles. What is the shape of the blue figure? MCC5.G.4



# **Inquiry Lab**

#### **Area of Irregular Figures**

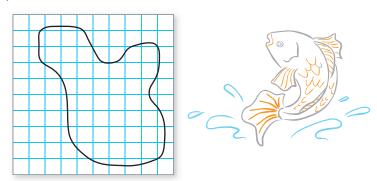


#### HOW can you estimate the area of an irregular figure?



1, 3, 4, 5

Ponds The Ramirez family is putting a koi pond in their backyard. They need to estimate the area of the pond to know how many fish they can put in the pond. A scale drawing of the pond is shown below. In the drawing, each square represents one square foot.



What do you know?		
_		

What do you need to know? _	
,	

#### **Investigation 1**

Step 1 Shade and count the number of whole squares the pond covers.

Step 2 Estimate the number of whole squares covered by the partial squares altogether.

Add your answers from Steps 1 and 2. Step 3

So, the area of the pond is about square feet.

#### Investigation 2

Another way to estimate the area of an irregular figure is to separate the figure into simpler shapes. Then find the sum of these areas.

Step 1

First, separate the figure into a triangle and a rectangle.

Step 2

Find the area of each figure.

Area of a triangle

$$A = \frac{1}{2}bh$$

$$= \frac{1}{2} \cdot 200 \cdot 311$$

$$= b = 300 - 100 \text{ or } 200$$

$$h = 481 - 170 \text{ or } 311$$

$$= 31,100$$
Simplify.

Area of rectangle

$$A = \ell w$$
  
= 300 • 170 or 51,000  $\ell = 300$  and  $w = 170$ 

Step 3

Add to find the total area.

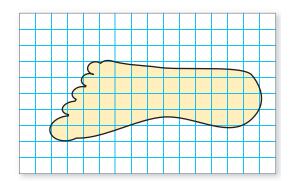
)	)	
+	=	

The area of Idaho is about square miles.

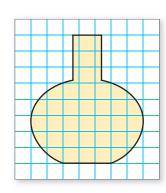


Use Math Tools Work with a partner to estimate the area of each irregular figure.

**1.** A ≈ \_\_\_\_\_



**2.** *A* ≈ \_\_



triangle

rectangle

481 mi

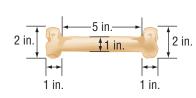
# Collaborate

Work with a partner to estimate the area of each irregular figure.

3.  $A \approx$ 



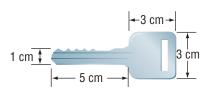
**4.** *A* ≈



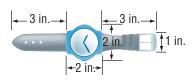
**5.** *A* ≈ \_\_\_\_



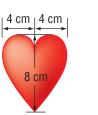
**6.** *A* ≈ \_\_\_\_\_



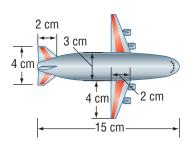
**7.** *A* ≈ \_\_\_\_\_



**8.** *A* ≈ \_\_\_\_\_



**9.** *A* ≈ \_\_\_\_\_



**10.** *A* ≈ \_\_\_\_





Work with a partner to complete the table. The first one is done for you.

	Irregular Figure	Draw the simpler shapes you can make.	Area of Each Simpler Shape	Estimated Area of Irregular Figure	
	4 cm → 12 cm →		$8 \times 3 = 24$ $12 \times 4 = 48$	72 square centimeters	
11.	6 in. ↓ <b>USA</b> ↓ 20 in. →			k	
12.	7 cm 5 cm 4 cm				
13.	2 in. 1 in. 2 in. 2 in. 3 in.				

14. Reason Inductively Heather solves Exercise 11 by subtracting the area of two triangles from the area of a large rectangle and finds the answer 105 square inches. How does Heather's answer compare to your answer for Exercise 11?



- **15.** Model with Mathematics Describe a real-world example of when it would be useful to estimate the area of a figure.
- 16. HOW can you estimate the area of an irregular figure?

# **Area of Composite Figures**

#### What You'll Learn

Scan the lesson. List two things real-world scenarios in which you would use the area of composite figures.



#### **Essential Question**

HOW does measurement help you solve problems in everyday life?



#### Vocabulary

composite figure



 $a_{b_C}$ 

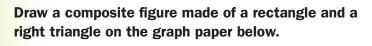
#### **Common Core GPS**

**Content Standards** MCC6.G.1

**Mathematical Practices** 1, 2, 3, 4, 6, 7

#### **Vocabulary Start-Up**

A composite figure is a figure made of two or more two-dimensional figures. The composite figure shown to the right is made of two rectangles.



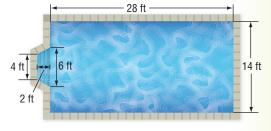




#### Real-World Link

**Pools** The dimensions of the city pool are shown.

1. What two-dimensional figures are used to make the shape of the pool?

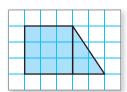


2. How could you determine the area of the pool floor?



## Find the Area of a Composite Figure

You can decompose some trapezoids into a square and a triangle to find the area.



Area of Square

$$A = \ell \cdot w$$

$$A = 3 \cdot 3$$
, or 9

Area of Triangle

$$A = \frac{1}{2}bh$$

$$A = \frac{1}{2}(2)(3)$$
, or 3

Then add the area of the square and the area of the triangle to find the area of the trapezoid. The area of the trapezoid is 9+3 or 12 square units.

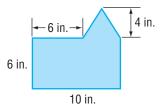
You can find the area of a composite figure using the same strategy. To find the area of a composite figure, separate it into figures with areas you know how to find. Then add those areas.

#### **Example**



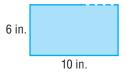
1. Find the area of the figure at the right.

The figure can be separated into a rectangle and a triangle. Find the area of each.



**Area of Rectangle** 

**Area of Triangle** 



$$A = \ell w$$

$$A = \frac{1}{2}bh$$

$$A = 10 \cdot 6 \text{ or } 60$$

$$A = \frac{1}{2}(4)(4)$$
 or 8

The base of the triangle is 10 - 6 or 4 inches.

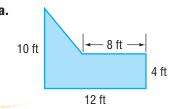
The area is 60 + 8 or 68 square inches.

Got It? Do these problems to find out.

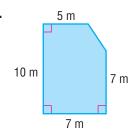
Find the area of each figure.

1

a.



b.



#### **Example**

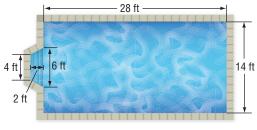


2. Find the area of the pool's floor.

Separate the figure into a rectangle and a trapezoid.

Rectangle:  $28 \times 14$  or 392Trapezoid:  $\frac{1}{2}(2)(4+6)$  or 10

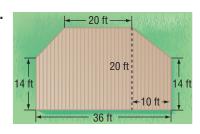
So, the area of the pool's



floor is 392 + 10 or 402 square feet.

Got It? Do this problem to find out.

C.





## Find the Area of Overlapping Figures

To find the area of overlapping figures, decompose the figures.

#### **Example**



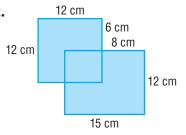
**3.** Find the area of the figure at the right.

Square:  $12 \times 12$  or 144Rectangle:  $15 \times 12$  or 180

The sum of the areas: 144 + 180 or 324

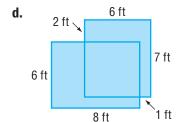
Overlapping area:  $6 \times 7$  or 42

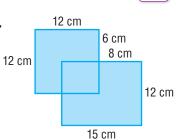
Subtract the overlapping area. 324 - 42 = 282



So, the area of the figure is 282 square centimeters.

Got It? Do this problem to find out.





**Be Precise** It is important not to count

the area of the overlapping portion twice when finding the area of overlapping figures.

#### **Example**



45 ft

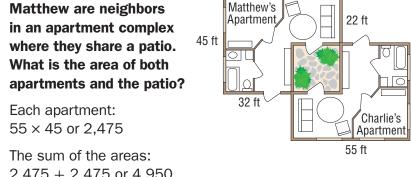
**Charlie and his brother Matthew are neighbors** in an apartment complex where they share a patio. What is the area of both apartments and the patio?

2,475 + 2,475 or 4,950

Patio: 23 × 23 or 529

Subtract the overlapping area. 4,950 - 529 = 4,421

So, the total area is 4,421 square feet.

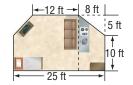


55 ft

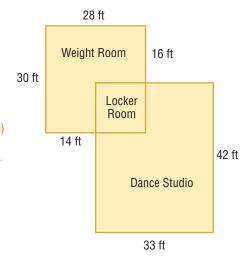
#### **Guided Practice**



1. The manager of an apartment complex will install new carpeting in a studio apartment. The floor plan is shown at the right. What is the total area that needs to be carpeted? (Example 1 and 2)



2. Finn Fitness has an entrance to the locker room from both the dance studio and the weight room. What is the total area of Finn Fitness? (Examples 3 and 4)



Building on the Essential Question How can you decompose figures to find area?

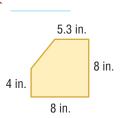


## Independent Practice

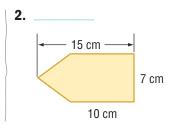


Find the area of each figure. Round to the nearest tenth if necessary. (Example 1)

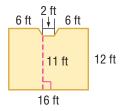
わ



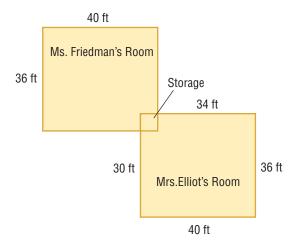
Show your work.



**3.** The floor plan of a kitchen is shown at the right. If the entire kitchen floor is to be tiled, how many square feet of tile are needed? (Example 2)



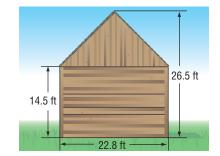
**4.** Ms. Friedman and Mrs. Elliot both teach sixth grade math. They share a storage closet. What is the total area of both rooms and the storage closet? (Examples 3 and 4)



The diagram shows one side of a storage barn.

**a.** This side needs to be painted. Find the total area to be painted.

Show your work.



**b.** Each gallon of paint costs \$20 and covers 350 square feet. Find the total cost to paint this side once. Justify your answer.

**6.** Reason Abstractly Refer to the graphic novel frame below for Exercises a–b.



- **a.** The first clue was hidden in a triangular section of the park with an area of 600 square feet. The second clue was hidden in a rectangular section with a height of 30 feet and a width of 24 feet. What was the area of the rectangular section?
- **b.** What is the total search area?

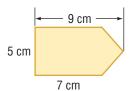


#### H.O.T. Problems Higher Order Thinking

7. Persevere with Problems Describe how to separate the figure into simpler figures. Then estimate the area. One square unit equals 2,400 square miles. Justify your answer.

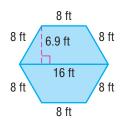


8. Colors Identify Structure Describe how you would find the area of the figure shown at the right.



#### **Georgia Test Practice**

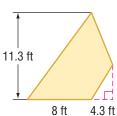
- **9.** The diagram gives the dimensions of the geodome climber on the playground. What is the total area of the geodome?
  - A 82.8 ft<sup>2</sup>
- © 331.2 ft<sup>2</sup>
- ® 165.6 ft<sup>2</sup>
- ① 883.2 ft<sup>2</sup>



#### **Extra Practice**

Find the area of each figure. Round to the nearest tenth if necessary.

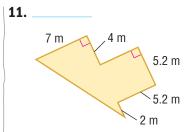
10. 69.5 ft<sup>2</sup>



$$A = \frac{1}{2}(8)(11.3) = 45.2$$

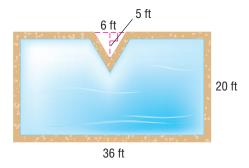
$$A = \frac{1}{2}(4.3)(11.3) \approx 24.3$$

$$45.2 + 24.3 = 69.5$$

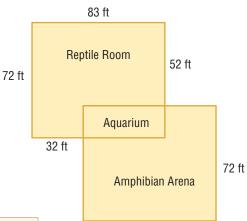


**12.** The diagram gives the dimensions of a swimming pool. If a cover is needed for the pool, what will be the

approximate area of the cover?



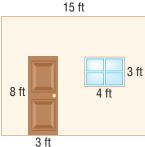
13. At the local zoo, the aquarium can be seen from the Reptile Room and the Amphibian Arena. What is the total area of both rooms and the aquarium?



14. Persevere with Problems

The diagram shows one wall of Sadie's living room.

a. This wall needs to be painted. 12 ft Find the total area to be painted.

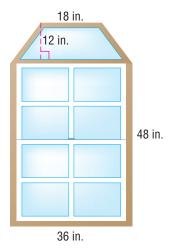


83 ft

b. Each quart of paint costs \$8 and covers 90 square feet. Find the total cost to paint this wall once. Justify your answer.

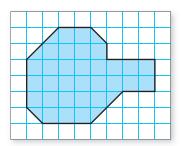
#### **Georgia Test Practice**

15. What is the area of the window shown?



- $\bigcirc$  2,052 in<sup>2</sup>
- © 508.68 in<sup>2</sup>
- B 1,728 in<sup>2</sup>
- ① 324 in<sup>2</sup>

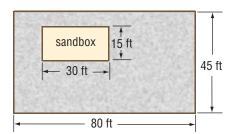
16. The shaded part of the grid represents the plans for a fish pond.



If each square on the grid represents 5 square feet, what is the approximate area of the fish pond?

- © 175 square feet
- © 165 square feet
- H 150 square feet
- ① 33 square feet
- 17. Short Response To promote recycling, the ground of the neighborhood playground shown is being covered by shredded tires. The sandbox will not be covered. What is the area, in square feet, of the shredded tire portion of

the playground?



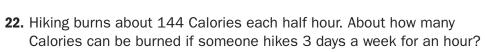
#### **Common Core Review**

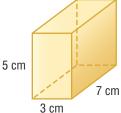
Multiply. MCC5.NBT.5

**18.** 
$$36 \times 12 =$$
 \_\_\_\_\_\_

**19.** 
$$15 \times 71 =$$

21. Find the volume of the rectangular prism. MCC5.MD.5b





MCC4.OA.3

# 2 ST CENTURY CAREER

# in Community Planning

#### **Parks and Recreation Planner**

Do you enjoy thinking about how your community might look 10 years in the future? If so, a career in parks and recreation planning might be a perfect fit for you. Most planners are employed by local governments. They assess the best use for the land and create short and long term plans for various parks and recreation areas. They make recommendations based on the location of roads, schools, and residential areas. A parks and recreation planner uses mathematics, science, and computer software to complete their work.



**Explore college and careers** at ccr.mcgraw-hill.com

#### Is This the Career for You?

Are you interested in a career as a parks and recreation planner? Take some of the following courses in high school.

- Economics
- Environmental Design
- Geometry

Turn the page to find out how math relates to a career in Community Planning.



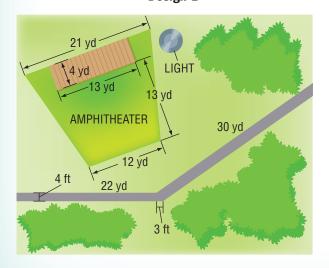
#### You be the Parks and Recreation Planner!

For each problem, use the information in the designs.

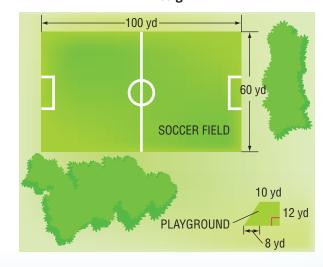
- 1. What is the area of the playground in Design 2?
- 2. In Design 2, how much larger is the area of the soccer field than the area of the playground?
- 3. In Design 1, the amphitheater has a stage. What is the area of the amphitheater without the stage?

4. The cost of building the amphitheater including the stage is \$225 a square yard. The budget provided to build the amphitheater is \$65,000. Are they within budget? Explain.

Design 1



Design 2



#### **Career Project**

It's time to update your career portfolio! The New York City Department of Parks and Recreation has a free "Park Planner Game" online. Go to the Website to create your own park with trees, sports fields, and paths, while trying to stay under budget.

What is something you really want to do in the next ten years?

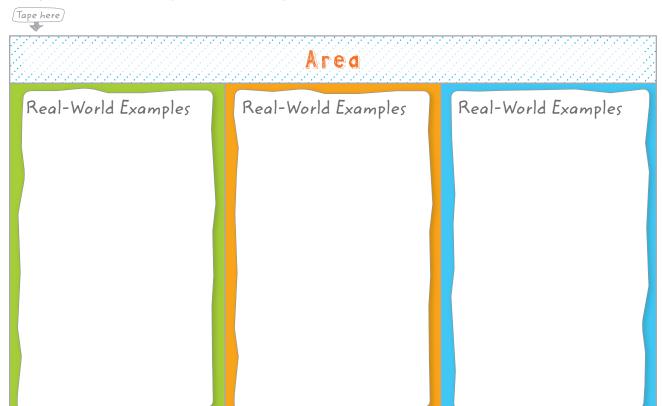
# **Vocabulary Check**

Uns	scramble each of t	he clue words.
SE	ЗА	
HG	ЕНТІ	
LYN	IPOOG	
LAE	EGARLAPLORM	
МН	OBRUS	
NE	TRUGNOC	
PO	MECSOTI ERFUGI	
AR	OMLUF	
Coi	mplete each sente	ence using one of the unscrambled words above.
1.	Α	is a simple closed figure formed by three or more straight line segments.
2.	The shortest dista	ance from the base of a parallelogram to its opposite side is
	the	
3.	Acongruent.	is a quadrilateral with opposite sides parallel and opposite sides
4.	. Any side of a parallelogram is a	
5.	A parallelogram with four congruent sides is a	
6.	If two shapes have the same measure they are	
7.	A figure made of t	riangles, quadrilaterals, and other two dimensional figures
	is a	
8.	Α	is an equation that shows a relationship among certain quantities.

#### **Key Concept Check**

#### Use Your FOLDABLES

Use your Foldable to help review the chapter.

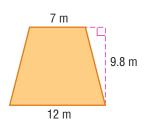


#### Got it?

Match each expression with correct steps used to find the area of the trapezoid.



- **2.** Replace *h* with 9.8.
- **3.** Replace  $b_1$  with 7 and replace  $b_2$  with 12.
- **4.** Add.
- **5.** Multiply.



**a.** 
$$A = \frac{1}{2}(9.8)(b_1 + b_2)$$

**b.** 
$$A = \frac{1}{2}bh$$

**c.** 
$$A = \frac{1}{2}(9.8)(19)$$

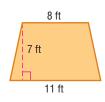
**d.** 
$$A = \frac{1}{2}h(b_1 + b_2)$$

**e.** 
$$A = 93.1$$

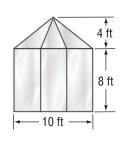
**f.** 
$$A = \frac{1}{2}(9.8)(7 + 12)$$

## **Problem Solving**

- **1.** Find the height of a deck if it is a parallelogram with base  $8\frac{1}{4}$  feet and an area of  $49\frac{1}{2}$  square feet. (Lesson 1)
- 2. How much material is needed to make a triangular flag with base  $2\frac{1}{4}$  feet and height  $8\frac{1}{2}$  feet? (Lesson 2)
- One room in Franco's room is in the shape of a trapezoid with the dimensions shown. Find the area of the wall to be painted. (Lesson 3)



- 4. Reason Abstractly A window is shaped like a trapezoid. The bases are 30 inches and 40 inches. The height of the window is 24 inches. Find the area of the window. (Lesson 3)
- **5.** A bricklayer wants to arrange 16 bricks into a rectangular shape with the greatest perimeter possible. How many bricks will be in each row? (PSI)
- 6. Clean length of 10 centimeters, and a width of 8 centimeters is multiplied by 0.5. Describe the change in the perimeter. (Lesson 4)
- 7. The side of a four season room is being constructed with the dimensions shown. Find the area of the side being built of glass windows. (Lesson 5)



# Reflect

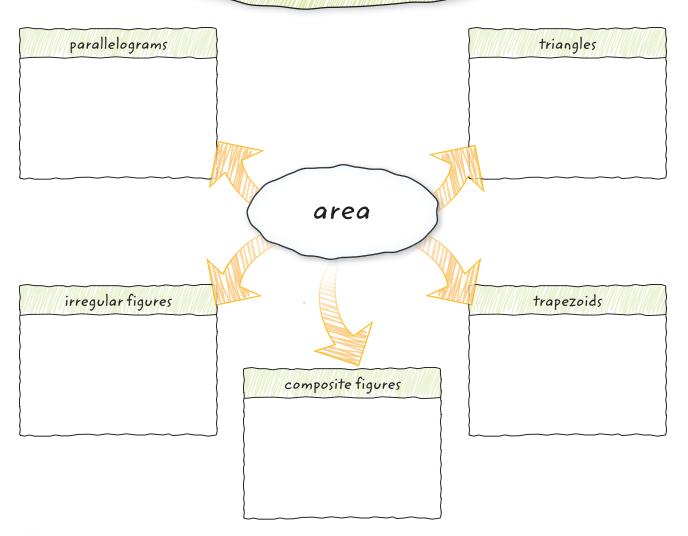


#### **Answering the Essential Question**

Use what you learned about area to complete the graphic organizer. List several real-world examples for each figure.



**HOW** does measurement help you solve problems in everyday life?





Answer the Essential Question. HOW does measurement help you solve problems in everyday life?